

**Proposition 3.1.** *If  $F_X$  is a distribution function, then*

1.  $\lim_{x \rightarrow -\infty} F_X(x) = 0$  and  $\lim_{x \rightarrow \infty} F_X(x) = 1$ .
2.  $F_X(x)$  is a nondecreasing function of  $x$ . That is, if  $s < t$ , then  $F_X(s) \leq F_X(t)$ .
3.  $F_X(x)$  is right continuous. That is, for every  $x_0$ ,

$$\lim_{\substack{h \rightarrow 0 \\ h > 0}} F_X(x_0 + h) = F_X(x_0).$$